

## Mathematics at ISUtrecht

**The Role Play phase can span from kindergarten to grade 2. A student is in the Role play phase when the student displays any of these indicators:**

- distinguish tallness, heaviness, opposites and how much things hold
- describe two or three obvious measurement attributes of the same thing
- describe something as having more or less of an attribute than something else, e.g. as being taller than or as being fatter than.
- look at displays of familiar data and say which is most or has more
- sort and arrange data they have collected into familiar groupings
- count when asked to say how many in each group in a data display
- use 'bigger', 'smaller' and 'the same' to describe differences between small collections
- anticipate whether an indicated change to a collection or quantity will make it bigger, smaller or leave it the same
- distinguish spoken numbers from other spoken words
- distinguish numerals from other written symbols
- see at a glance how many are in small collections and attach correct number names to such collections
- connect the differences they see between collections of one, two and three with the number string: 'one, two, three, ...'
- understand a request to share in a social sense and distribute items or portions.
- recall the sequence of number names at least into double digits
- know how to count a collection, respecting most of the principles of counting
- understand that it is the last number said which gives the count
- understand that building two collections by matching one to one leads to collections of equal size, and can 'fix' one collection to make it match another in size
- compare two collections one to one
- solve small number story problems which require them to add some, take some away, or combine two amounts by imagining or role playing the situation and counting the resulting quantity
- share by dealing out an equal number of items
- distinguish shape from other attributes that relate to how things 'look'
- use informal language that indicates they are responding to shape; e.g. 'the pointy one'
- carry out matching tasks by selecting a matching shape from a collection and either posting shapes in boxes or fitting shapes into cut outs

- reproduce simple geometric configurations if only encoding is required; that is, build a matching shape or arrangement to one that is constantly in sight
- draw simple figures by imitating how they have seen them drawn (including letters and numbers)
- give directions from one landmark to the next when retelling a journey or places in a story; e.g. 'go to the pond, go on the bridge, go home'.

**The Experimental phase can span from kindergarten to grade 3. In the Experimental phase for mathematics, the student demonstrates all the following indicators:**

- know that several things may be in different orders when compared by different attributes
- line up the base of two sticks when comparing their lengths and fit regions on top of each other to compare area
- use the everyday notion of 'how many fit' and count how many repeats of an object fit into or match another; e.g. How many pens fit along the table?
- count units and call it 'measuring'; e.g. I measured and found the jar holds a bit more than 7 scoops.
- use 'between' to describe measurements quantities (length, mass, capacity, time); e.g. It weighs between 7 and 8 marbles.
- understand expressions such as "will happen," "won't happen," and "might happen"
- distinguish impossible events from events that are possible but unlikely
- suggest counting as a way of answering data questions that focus on comparing collections
- use skip counting to say how many in a tally
- use counting to help construct their data display, e.g., construct a block graph by counting how many in each group, then counting how many squares to colour in
- understand the need for a baseline and space blocks regularly to allow comparisons to be made
- place direct measurement data in sensible sequences using a baseline, e.g., cut paper strips to fit around their heads and make a bar (column) graph by lining up the bottom of strips
- choose to count to compare the sizes of groups, without prompting
- look at a bar graph and say which bar has more based on its length
- describe figures and objects using terms that are evocative of shape, such as 'corner', 'pointy', 'lopsided', 'slanty'
- describe conventional figures and objects by reference to prototypes they 'look like'; e.g. 'It's a door shape'.

- select ready-made materials that 'look right' to make recognisable models of parts of their environment
- remember what some families of shapes look like and produce recognisable versions
- remember key aspects of the way things look and try to reproduce them in their drawings; e.g. drawing circles for wheels, putting two eyes, a nose and a mouth on a face
- relate the position of objects to each other in familiar settings using terms such as 'behind', 'near'
- draw or make simple 'route' maps and models that show a sense of spatial relationships and order, although only for local settings that they have freely explored.

**The Early phase can span from grade 1 to grade 5. In the Early phase for mathematics, the student demonstrates all the following indicators:**

- directly compare and order events from more to less likely and are able to justify their decision with relevant reasons.
- understand what it means for simple events to be equally likely
- see that, when organising data, the categories can be reorganised without changing the overall total
- produce and read pictographs or block graphs where each unit represents more than one piece of data
- produce simple two-way tables and Venn diagrams, partitioning totals between the cells or sections for straightforward data
- represent whole-number data in different ways
- use column and row headings to interpret what the numbers in simple two-way tables represent
- connect the repetition of a 'unit' with the numbers on a whole-number calibrated scale
- make things to a specified length in uniform units (including centimetres and metres)
- use provided measurements to make a decision about comparative size
- count units as a strategy to solve comparison problems such as: Whose frog is heavier?
- say which is longer (heavier) based on information about the number of units matching each object
- select counting as a strategy to solve problems such as: Are there enough cups? Who has more? Will it fit?
- use materials or visualise to decompose small numbers into parts empirically; e.g. 8 is the same as 5 with 3
- make sense of the notion that there are basic facts
- select either counting on or counting back for subtraction problems depending on which strategy best matches the situation

- think of addition and subtraction situations in terms of the whole and the two parts and which is missing
- write number sentences that match how they think about the story line for small number addition and subtraction problems
- respond to a request to 'tell me about the shape of this ...' using language such as 'flat', 'curved', 'side', 'round', 'face', 'edge', 'square', 'angle', 'base'
- compare and contrast geometric figures
- identify the faces, edges and vertices of a geometric object and hence select component parts to make it in various forms (skeletal, hollow)
- match the 2D shapes with the faces of standard 3D shapes
- select nets that have the right component parts to match a simple object
- recognise repetitions of the same shape embedded within arrangements and patterns
- identify component parts to show that a shape or arrangement is symmetrical
- describe one thing being between others and put key features in order on a map

**The Transitional phase can span from grade 3 to secondary. In the Transitional phase for mathematics, the student demonstrates all the following indicators:**

- draw on numerical information alone to decide whether two simple events are or are not equally likely to occur
- systematically list all possibilities, unprompted, to work out numerical probabilities for one-stage actions
- use experimental results and data about past events to determine a range of possible outcomes and informally use relative frequency to estimate probabilities
- create axes that show discrete or continuous quantities, including time scales
- use simple proportional comparisons when interpreting data in tables and graphs, e.g., half as many people prefer pizzas to hamburgers
- use part-whole reasoning without needing to see or visualise physical collections.
- compose 'part-units' into wholes, understanding, for example, that a narrow garden bed may have an area of 5 or 6 square metres even though no whole 'metre squares' fit into the bed

- compare whole numbers using their knowledge of the patterns in the number sequence, and think of movements between numbers without actually or mentally representing the numbers as physical quantities
- partition at least two- and three-digit numbers into standard component parts (e.g.  $326 = 300 + 20 + 6$ ) without reference to actual quantities
- write suitable number sentences for the range of addition and subtraction situations
- use the inverse relationship between addition and subtraction to make a direct calculation possible
- double count in multiplicative situations by representing one group and counting repetitions of that same group, simultaneously keeping track of the number of groups and the number in each group
- use successive splits to show that one half is equivalent to 2 parts in 4, 4 parts in 8, etc. and expect that if the number of portions is doubled, they halve the size of each portion
- give a detailed list of properties in their descriptions of shapes
- know from the properties of a rectangle that a slanted parallelogram cannot be a rectangle even though it is what a rectangular face on a block 'looks like' from 'the side'
- use mathematical conventions to represent objects in different types of drawings
- produce their own nets for geometric shapes that they can see and handle
- describe characteristic features of mirror symmetry
- identify the particular rotations, reflections and translations that relate the component parts of simple arrangements and patterns

**The Conventional phase can span from grade 4 to secondary. In the Conventional phase for mathematics, the student demonstrates all the following indicators:**

- develop coordinated mental representations of spatial configurations
- understand why the area of a rectangle and the volume of a rectangular prism can be found by multiplying its length dimensions and can use this for fractional side lengths
- think of the part-units themselves as units; e.g. a particular unit can be divided into one hundred parts and each part is then a centi-unit
- subdivide units to make measurements more accurate
- choose units that are sufficiently small (that is, accurate) to make the needed comparisons
- use their understanding of the multiplicative structure built into the metric system to move flexibly between related standard units; e.g. they interpret the 0.2 kilogram mark on a scale as 200 grams

- use relationships between measurements to find measures indirectly; e.g. knowing that  $1 \text{ mL} = 1 \text{ cm}^3$  they can find the volume of an irregular solid in cubic centimetres by finding how many millilitres of water it displaces using a capacity cylinder
- use a range of information sources to put things in order from least likely to most likely, e.g., use research data or experimental data to form conclusions
- interpret the 0 to 1 scale in general usage and understand why the probability that a toss of a fair die will produce 5 is one-sixth
- use their knowledge that, for example, the 2 being in the tens place in 426 tells us that it refers to two groups of ten, to generate alternative partitions
- find it obvious that if 3 rows of 5 is 15, then both 15 divided by 3 and one third of 15 are 5
- visualise or draw their own diagrams to compare fractions with the same denominator (e.g.  $\frac{3}{7}$  and  $\frac{5}{7}$ ) or simple equivalences (e.g.  $\frac{1}{2}$  and  $\frac{2}{4}$ )
- use the idea of splitting a whole into parts to understand, for example, that 2.4 is  $2 + \frac{4}{10}$  and 2.45 is  $2 + \frac{45}{100}$
- relate fractions and division knowing, for example, that  $\frac{3}{4}$  can be thought of as  $3 \div 4$  and 3 things shared among 4 students has to be  $\frac{3}{4}$
- select an appropriate multiplication or division operation on whole numbers including for problems that are not easily interpreted as 'lots of'; e.g. combination and comparison problems
- use properties to convince themselves and others why a figure or object belongs to a class; e.g. This is a square because it has four equal sides even though it is not resting on a 'flat bottom'.
- understand relationships between properties of figures; e.g. if a triangle has two equal angles then it has two equal sides
- produce their own nets, considering in advance the level of precision needed to ensure the shape is correct in form and size, where tabs will be, and so on
- predict the effect of particular movements (translations, rotations and reflections) on the orientation and position of figures and objects